Write your name here


| Mathematics |  |
| :--- | :---: |
| Paper 1 (Non-Calculator) | Model <br> Solutions |
|  | Foundation Tier |
| Sample Assessment Materials I Issue 2 <br> Time: 1 hour 30 minutes | Paper Reierence <br> 1MA1/1F |

You must have: Ruler graduated in centimetres and millimetres, Total Marks protractor, pair of compasses, pen, HB pencil, eraser.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
-     - there may be more space than you need.

Calculators may not be used.


- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

The total mark for this paper is 80

- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL questions.

## Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Write the following numbers in order of size.
Start with the smallest number.
0.61
0.1
0.16
0.106
$0.1,0.106,0.16,0.61$

2 Write 0.037 as a fraction.


3 Write down the 20th odd number.
$1,3,5,7$ and on and on
The sequence for odd numbers is $2 n-1$
So $2(20)-1$ is roth odd number.

$$
\begin{equation*}
=40-1=39 \tag{39}
\end{equation*}
$$

4 Write down all the factors of 20


$$
1,2,4,5,10,20
$$

5 Tanya needs to buy chocolate bars for all the children in Year 7
Each of the 130 children get one chocolate bar.
There are 8 chocolate bars in each packet.
Work out the least number of packets of chocolate bars that Tanya needs to buy.
$1 \times 130=130$ chocolates
$\frac { 1 3 0 } { 8 } \rightarrow 8 \longdiv { 0 1 6 \cdot 2 5 } = 1 6 . 2 5$
So 17 packets needed as Greg can only buy a whole number of packets.

6 Greg rolls a fair ordinary dice once.
(i) On the probability scale, mark with a cross $(\times)$ the probability that the dice will land on an odd number. $\quad(1) 2,3), 4,(3), 6 \rightarrow 3 / 6$ are odd $=1 / 2$


(ii) On the probability scale, mark with a cross $(\times)$ the probability that the dice will land on a number less than $5 \quad 1,2,3,4,5,6 \rightarrow \frac{4}{6}$ numbers less than 5. |  | 1 |  | $X$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $1 / 6$ | $2 / 6$ | $\frac{1}{2}=\frac{3}{6}$ | $4 / 6$ | $5 / 6$ |

7 One day Sally earned $£ 60$
She worked for 8 hours.
Work out Sally's hourly rate of pay.

$$
\frac{\epsilon 60}{8}=\frac{60}{8}=\frac{30}{4}=\frac{15}{2}=67.5 \text { per hour }
$$

£ 7.50

8 Work out $15 \%$ of 80
$\left.\begin{array}{l}\div 10\left(\begin{array}{l}100.10=80 \\ \\ 10.10=8\end{array} \longrightarrow \div 10\right. \\ \hline 5.10=4\end{array}\right) \div 2$
$\begin{aligned} 10.1 \cdot+5.1 & =15.10 \\ 8+4 & =12\end{aligned}$

9 There are 3 red beads and 1 blue bead in a jar.
A bead is taken at random from the jar.
What is the probability that the bead is blue?

$$
3+1=4 \text { total beads. }
$$

1 is slue so $1 / 4$.

10 There are only black pens and green pens in a box.
The ratio of the number of black pens in the box to the number of green pens in the box is $2: 5$

What fraction of the pens are black?
Total parts $\rightarrow 2+5=7$
2 parts are black $\rightarrow 2 / 7$

11 Sally has three tiles.
Each tile has a different number on it.
Sally puts the three tiles down to make a number. Each number is made with all three tiles.


How many different numbers can Sally make?


12 Here are the first three patterns in a sequence.
The patterns are made from triangles and rectangles.

pattern number

pattern number 2

pattern number 3
(a) How many triangles are there in pattern number 7 ?

$$
\begin{array}{r}
\underbrace{6,810}_{+2}+2 \rightarrow \begin{array}{c}
\text { sequence is going up in } 2 \text { so } 2 n . \\
\text { number before } 6 \text { would be } 4 \text { so } 2 n+4 \\
2 n+4 \rightarrow 2(7)+4=18
\end{array}
\end{array}
$$

Charlie says
"There are 4 rectangles in pattern number 3 so there will be 8 rectangles in pattern number 6 "
(b) Is Charlie right?

Give a reason for your answer.

The pattern fer the rectangles is pattern number +1 . So for $8^{\text {th }}$ pattern $\rightarrow 8+1=9$ rectangles. $\qquad$
So Charlie is incorrect.

13 Paul organised an event for a charity.
Each ticket for the event cost $£ 19.95$
Paul sold 395 tickets.
Paul paid costs of $£ 6000$
He gave all money left to the charity.
(a) Work out an estimate for the amount of money Paul gave to the charity.
$\begin{aligned} \text { Money made from tickets } & \rightarrow \in 19.95 \times 395 \\ & \rightarrow \in 20.00 \times 400=€ 8000\end{aligned}$
costs 66000
So money to charity $\rightarrow t 8000-t 6000=+2000$
(b) Is your answer to (a) an underestimate or an overestimate?

Give a reason for your answer.
Overestimate as both numbers rounded up and then multiplied.

14 The table shows information about the numbers of fruit trees in an orchard.

| Apple tree | Pear tree | Plum tree |
| :---: | :---: | :---: |
| 45 | 20 | 25 |

(a) The pictogram shows this information

Use plum tree to work out.
Complete the key for the pictogram. $\quad 5 \Delta=25 \rightarrow \frac{25}{5}=\Delta=5$


Key: $\triangle$ represents .5 .. trees
(b) There are 90 fruit trees in the orchard.

| Apple tree | Pear tree | Plum tree |
| :---: | :---: | :---: |
| 45 | 20 | 25 |

Draw an accurate pie chart for this information.
Pear trees $\rightarrow \frac{20}{90}=\frac{2}{9}$


$$
1 / 2 \times 360^{\circ}=180^{\circ}
$$

(Total for Question 14 is 4 marks)

15 Carpet tiles are going to be used to cover a floor.
The floor is a 1200 mm by 1000 mm rectangle.
Each carpet tile is a 40 cm by 30 cm rectangle.
Exactly 10 carpet tiles can be used to cover the floor completely.
Show in a labelled sketch how this can be done.
$1200 \mathrm{~mm}=120 \mathrm{~cm} \quad 1000 \mathrm{~mm}=100 \mathrm{~cm}$


16 Sam buys 20 boxes of oranges.
There are 25 oranges in each box.
Each boxes of oranges costs $£ 7$
Sam sells $2 / 5$ of the oranges he bought.
He sells each of these oranges for 40p.
He then sells each of the remaining oranges at 3 oranges for 50p.
Did Sam make a profit or did Sam make a loss?
You must show working to justify your answer.
Token Oranges bought $\rightarrow 20 \times 25=500$
Money spent $\longrightarrow 20 \times t 7=t 140$
Sold $2 / 5$ of 500 oranges $\rightarrow 200$

$$
200 \times 60.40=680 \text { made }
$$

Remaining 300 oranges sold in 3's $\rightarrow \frac{300}{3}=100$ batches

$$
100 \times t 0.50=t 50 \text { made } .
$$

Toter made $\rightarrow \in 80+E 50=E 130$
Money spent $\rightarrow \in 140$
Profit $\rightarrow$ made - spent $\rightarrow t 130-t 140=-t 10$

Negative answer so Sam made loss of 610 .

17100 students had some homework.
42 of these students are boys.
8 of the 100 students did not do their homework.
53 of the girls did do their homework.
(a) Use this information to complete the frequency tree.


One of the girls is chosen at random.
(b) Work out the probability that this girl did not do her homework.

## 5 girls out of 58 didut

5/58

18 (a) Work out $2 / 7+1 / 5$

$$
\begin{aligned}
& 5 \times 7=35 \text { which is LCM so use as common denominator. } \\
& \frac{2 \times 5}{7}=\frac{10}{35} \\
& \frac{10}{35}+\frac{7}{35}=\frac{17}{35}
\end{aligned}
$$

(b) Work out $12 / 3 \div 3 / 4$

$$
\begin{aligned}
& 1 \frac{2}{3} \div \frac{3}{4} \\
& 1 \frac{2}{3} \rightarrow \frac{3}{3}+\frac{2}{3}=\frac{5}{3} \\
& \frac{5}{3} \div \frac{3}{4} \rightarrow \frac{5}{3} \times \frac{4}{3}=\frac{20}{9}
\end{aligned}
$$

19 Solve $4 x+5=x+26$

$$
\begin{aligned}
& 4 x+5=x+26 \\
& 3 x+5=26 \\
& 3 x=21 \\
& x=7
\end{aligned}
$$

20 In a sale, normal prices are reduced by $20 \%$.
The normal price of a coat is reduced by $£ 15$
Work out the normal price of the coat.


21 Work out $6.34 \times 5.2$


22 Expand and simplify $(m+7)(m+3)$

$$
\begin{aligned}
& (m+7)(m+3) \\
& m^{2}+7 m+3 m+21 \\
& m^{2}+10 m+21
\end{aligned}
$$

$$
m^{2}+10 m+21
$$

23

$A E, D B G$ and $C F$ are parallel.
$D A=D B=D C$.
Angle $E A B=$ angle $B C F=38^{\circ}$
Work out the size of the angle marked $x$.
You must show your working.
$\angle A B D=38^{\circ}$ and $\angle C B D=38^{\circ}$ because alternate angles equal $\angle D A B=38^{\circ}$ and $\angle D C B=38^{\circ}$ because base angles equal in isoceles.

$$
\begin{aligned}
\angle A D B=\angle C D B & =180-2(38) \\
& =180-76 \\
& =104^{\circ}
\end{aligned}
$$

Angles around a point add to $360^{\circ}$ :

$$
x=360-2(104)
$$

$$
=360-208
$$

$$
=152^{\circ}
$$

24 Gary drove from London to Sheffield.
It took him 3 hours at an average speed of $80 \mathrm{~km} / \mathrm{h}$.
Len drove from London to Sheffield.
She took 5 hours.
Assuming that Len
drove along the same roads as Gary
 and did not take a break,
(a) work out Lyn's average speed from London to Sheffield.
$S_{\text {peed }}=\frac{\text { distance }}{\text { time }} \quad$ Distance $=$ speed $\times$ time
Gory distance $\rightarrow 80 \times 3=240 \mathrm{~km}$
Lyn speed $\rightarrow \frac{240}{5}=\underline{\underline{48 k m} / \mathrm{h}}$
(b) If Lyn did not drive along the same roads as Gary, explain how this could affect your answer to part (a).
It means she would had travelled a different
distance to bars so her average speed would be different.

25 In a company, the ratio of the number of men to the number of women is 3:2
$40 \%$ of the men are under the age of 25
$10 \%$ of the women are under the age of 25
What percentage of all the people in the company are under the age of 25 ?
Total ports $=2+3=5$
40d. of men $\rightarrow 0.4 \times 3=1.2 \longrightarrow 1.2+0.2=1.4$
10 d . of women $\rightarrow 0.1 \times 2=0.2$

$$
\frac{1.4}{5}=\frac{14}{50}=\frac{28}{100}=28.10
$$

26 The plan, front elevation and side elevation of a solid prism are drawn on a centimetre grid.

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

In the space below, draw a sketch of the solid prism.
Write the dimensions of the prism on your sketch.


27 There are 1200 students at a school.
Kate is helping to organise a party.
She is going to order pizza.
Kate takes a sample of 60 of the students at the school.
She asks each student to tell her one type of pizza they want.
The table shows information about her results.

| Pizza | Number of students |
| :---: | :---: |
| ham | 20 |
| salami | 15 |
| vegetarian | 8 |
| margarita | 17 |

Work out how much ham pizza Kate should order.
Write down any assumption you make and explain how this could affect your answer.

$$
\frac{20}{60} \text { wanted ham pizza }=1 / 3
$$

$1 / 3 \times 1200=400$ ham pizzas

I assumed the sample is representative of the Th le population.

28 Here is a parallelogram.


Work out the value of $x$ and the value of $y$.

$$
5 x-20=2 x+43 \text { because opposite angles of parallelogram }
$$

$$
3 x=63
$$

$$
x=21
$$

Angles on same side add to $180^{\circ}$
$(5 x-20)+(4 y-5 x)=180^{\circ}$
$(105-20)+(45-105)=180^{\circ}$
$85+45-105=180$
$45=200$
$y=50^{\circ}$

$$
x=\quad 21^{\circ}
$$

$=50^{\circ}$


Describe fully the single transformation that maps triangle A onto triangle B.
Rotation $90^{\circ}$ clockwise about $(0,0)$
$30 \mathbf{a}=\binom{3}{-7} \quad \mathbf{b}=\binom{4}{2}$
Work out $\mathbf{b}-2 \mathbf{a}$ as a column vector.

$$
\binom{4}{2}-2\binom{3}{-7}=\binom{4}{2}-\binom{6}{-14}=\binom{-2}{16}
$$

